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Exam. Code : 103202

Subject Code : 1025

B.A./B.Sc. 2nd Semester

MATHEMATICS

Paper—I (Calculus and Differential Equations)

Time Allowed—2 Hours] [Maximum Marks—50

Note :— There are *eight* questions of equal marks. Candidates are required to attempt any *four* questions.

1. (a) Show that the asymptotes of the curve :
$$x^4 - 5x^2y^2 + 4y^4 + x^2 - y^2 + x + y + 1 = 0$$
Cut the curve in atmost eight points which lie on a rectangular hyperbola.
(b) Find the intervals in which the curve
 $y = (\cos x + \sin x)e^x$ is concave upwards or downwards in $(0, 2\pi)$. Find also the points of inflexion.
2. (a) Find the position and nature of double points on the curve :
$$(2y + x + 1)^2 - 4(1 - x)^5 = 0$$
(b) Trace the curve $x^3 + y^3 = 3axy$, $a > 0$. 5+5=10
3. (a) Evaluate $\int \frac{\cosh x + \sinh x}{\cosh^2 x + \sinh^2 x} dx$

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(Contd.)

(b) Prove that

$$\frac{2}{\pi} \int_0^{\pi/2} \frac{1}{\sqrt{1-e^2 \sin^2 x}} dx = 1 + \frac{1^2}{2^2} e^2 + \frac{1^2 \cdot 3^2}{2^2 \cdot 4^2} e^4 + \frac{1^2 \cdot 3^2 \cdot 5^2}{2^2 \cdot 4^2 \cdot 6^2} e^6 + \dots$$

where $0 < e < 1$.

4. (a) Find the entire length of the curve $\left(\frac{x}{a}\right)^{\frac{2}{3}} + \left(\frac{y}{b}\right)^{\frac{2}{3}} = 1$.

(b) Prove that the area of the curve $a^4 y^2 = x^5(2a-x)$ to that of a circle of radius 'a' ($a > 0$) is as 5 : 4.

5. (a) Solve $x^2 - \frac{xy}{p} = f(y^2 - xyp)$ where $p = \frac{dy}{dx}$.

(b) Solve $(xy^2 + 2x^2y^3)dx + (x^2y - x^3y^2)dy = 0$.

6. (a) Find the complete primitive and singular solution

$$\text{of } (a^2 - x^2) \left(\frac{dy}{dx}\right)^2 + 2xy \frac{dy}{dx} + (b^2 - y^2) = 0.$$

(b) Show that the orthogonal trajectory of a system of concurrent straight lines is a system of concentric circles and conversely.

7. (a) Solve $(D^2 - 3D + 2)y = \cos(e^{-x})$ where $\frac{d}{dx} = D$ by method of variation of parameters.

(b) Solve $\frac{d^4 y}{dx^4} - y = x^2 \sin x$.

8. (a) Solve in series the differential equation :

$$x^2 \frac{d^2 y}{dx^2} + x \frac{dy}{dx} + \left(x^2 - \frac{1}{16}\right)y = 0$$

(b) Solve the differential equation :

$$(x^2 D^2 + 3xD + 1)y = (1-x)^{-2} \text{ where } D = \frac{d}{dx}.$$